Appendix: AP Physics 1 and 2 Equations and Constants

Table of Information and Equation Tables for AP Physics 1 and 2 Exams

The accompanying Table of Information and equation tables will be provided to students when they take the AP Physics 1 and 2 Exams. Therefore, students may NOT bring their own copies of these tables to the exam room, although they may use them throughout the year in their classes in order to become familiar with their content. The headings list the effective date of the tables. That date will only be changed when there is a revision to any of the tables. Check the Physics course home pages on AP Central for the latest versions of these tables (apcentral.collegeboard.org).

The Table of Information and the equation tables are printed near the front cover of <u>both</u> the multiple-choice section and the free-response section. The Table of Information is identical for both exams except for some of the conventions.

The equations in the tables express the relationships that are encountered most frequently in the AP Physics 1 and 2 courses and exams. However, the tables do not include all equations that might possibly be used. For example, they do not include many equations that can be derived by combining other equations in the tables. Nor do they include equations that are simply special cases of any that are in the tables. Students are responsible for understanding the physical principles that underlie each equation and for knowing the conditions for which each equation is applicable.

The equation tables are grouped in sections according to the major content category in which they appear. Within each section, the symbols used for the variables in that section are defined. However, in some cases the same symbol is used to represent different quantities in different tables. It should be noted that there is no uniform convention among textbooks for the symbols used in writing equations. The equation tables follow many common conventions, but in some cases consistency was sacrificed for the sake of clarity.

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Some explanations about notation used in the equation tables:

- 1. The symbols used for physical constants are the same as those in the Table of Information and are defined in the Table of Information rather than in the right-hand columns of the equation tables.
- 2. Symbols with arrows above them represent vector quantities.
- 3. Subscripts on symbols in the equations are used to represent special cases of the variables defined in the right-hand columns.
- 4. The symbol Δ before a variable in an equation specifically indicates a change in the variable (e.g., final value minus initial value).
- 5. Several different symbols (e.g., d, r, s, h, ℓ) are used for linear dimensions such as length. The particular symbol used in an equation is one that is commonly used for that equation in textbooks.

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ADVANCED PL	ACEMENT PHY	SICS 1 TABLE	E OF INFORMATI	ON, EFFECTIVE 2015
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	CONSTANTS AND CONVERSION FACTORS									
Proton mass, $m_p = 1.67 \times 10^{-27}$ kg				kg j	Electron	charge magnitud	e, <i>e</i> =	$1.60 \times 10^{-19} \text{ C}$		
Neutron mass, $m_n = 1.67 \times 10^{-27} \text{ kg}$			kg	Coulomb's law constant, $k = 1/4\pi\varepsilon_0 = 9.0 \times 10^9$ No			$N \cdot m^2/$	C^2		
Electron mass, $m_e = 9.11 \times 10^{-31} \text{ kg}$			cg	Universal gravitational constant, $G = 6.67 \times 10^{-11} \text{ m}^3/\text{kg} \cdot \text{s}^2$			g•s ²			
Speed of light, $c = 3.00 \times 10^8 \text{ m/s}$			ı/s	Accelera	tion due to gravit at Earth's surfac	ty e, g=	$= 9.8 \text{ m/s}^2$			
		meter,	m	kelvin,	K	watt,	W	degree Celsius,	°C	
	UNIT	kilogram,	kg	hertz,	Hz	coulomb,	С			
	SYMBOLS	second,	S	newton,	Ν	volt,	V			
		ampere,	А	joule,	J	ohm,	Ω			

PREFIXES					
Factor	Prefix	Symbol			
10 ¹²	tera	Т			
10 ⁹	giga	G			
10 ⁶	mega	М			
10 ³	kilo	k			
10^{-2}	centi	с			
10^{-3}	milli	m			
10 ⁻⁶	micro	μ			
10 ⁻⁹	nano	n			
10^{-12}	pico	р			

VALUES OF TRIGONOMETRIC FUNCTIONS FOR COMMON ANGLES							
θ	0°	30°	37°	45°	53°	60°	90°
$\sin \theta$	0	1/2	3/5	$\sqrt{2}/2$	4/5	$\sqrt{3}/2$	1
$\cos\theta$	1	$\sqrt{3}/2$	4/5	$\sqrt{2}/2$	3/5	1/2	0
$\tan \theta$	0	$\sqrt{3}/3$	3/4	1	4/3	$\sqrt{3}$	8

The following conventions are used in this exam.

- I. The frame of reference of any problem is assumed to be inertial unless otherwise stated.
- II. Assume air resistance is negligible unless otherwise stated.
- III. In all situations, positive work is defined as work done on a system.
- IV. The direction of current is conventional current: the direction in which positive charge would drift.
- V. Assume all batteries and meters are ideal unless otherwise stated.

MEC	THANICS	ELECTRICITY		
$v_x = v_{x0} + a_x t$	a = acceleration d = distance E = energy	$\left \vec{F}_{E}\right = k \frac{\left q_{1}q_{2}\right }{r^{2}}$	A = area F = force I = current	
$x = x_0 + v_{x0}t + \frac{1}{2}a_xt$ $v_x^2 = v_{x0}^2 + 2a_x(x - x_0)$	f = frequency F = force h = height	$I = \frac{\Delta q}{\Delta t}$	ℓ = length P = power q = charge	
$\vec{a} = \frac{\sum \vec{F}}{m} = \frac{\vec{F}_{net}}{m}$	I = rotational inertia K = kinetic energy k = contact on the second sec	$R = \frac{\rho c}{A}$ $I = \frac{\Delta V}{\Delta V}$	q = charge R = resistance r = separation t = time	
$\left \vec{F}_{f}\right \leq \mu \left \vec{F}_{n}\right $	l = length	R $P = I \Delta V$ $P = \sum P$	V = electric potential $\rho = \text{ resistivity}$	
$a_c = \frac{v^2}{r}$	m = mass P = power p = momentum	$R_s = \sum_i R_i$ $\frac{1}{2} = \sum_i \frac{1}{2}$		
$p = mv$ $\Delta \vec{p} = \vec{F} \Delta t$	r = radius or separation T = period t = time	$R_p = \frac{\sum_i R_i}{\sum_i R_i}$		
$K = \frac{1}{2}mv^2$	U = potential energy V = volume v = speed	W f -	AVES	
$\Delta E = W = F_{\parallel}d = Fd\cos\theta$	W = work done on a system x = position $\alpha =$ angular acceleration	$\lambda = \frac{v}{f} \qquad \begin{array}{c} J = -\frac{1}{2} \\ v = -\frac{1}{2} \\ \lambda = -\frac{1}{2} \end{array}$	speed wavelength	
$P = \frac{1}{\Delta t}$	μ = coefficient of friction	GEOMETRY AN	D TRIGONOMETRY	
$\theta = \theta_0 + \omega_0 t + \frac{1}{2}\alpha t^2$	θ = angle ρ = density	Rectangle $A = bh$	A = area C = circumference V = volume	
$\omega = \omega_0 + \alpha t$ $x = A\cos(2\pi tt)$	τ = torque ω = angular speed	Triangle $A = \frac{1}{2}bh$	S = surface area b = base	
$\vec{\alpha} = \frac{\sum \vec{\tau}}{I} = \frac{\vec{\tau}_{net}}{I}$	$\Delta U_g = mg \Delta y$ $- 2\pi 1$	Circle	h = height $\ell = \text{length}$ w = width	
$\tau = r_{\perp}F = rF\sin\theta$	$T = \frac{1}{\omega} = \frac{1}{f}$	$A = \pi r^2$ $C = 2\pi r$	r = radius	
$L = I\omega$ $\Delta L = \tau \Delta t$	$T_s = 2\pi \sqrt{\frac{m}{k}}$	Rectangular solid $V = \ell w h$	Right triangle $c^2 = a^2 + b^2$	
$K = \frac{1}{2}I\omega^2$	$T_p = 2\pi \sqrt{\frac{\iota}{g}}$	Cylinder $V = \pi r^2 \ell$	$\sin\theta = \frac{a}{c}$ $\cos\theta = \frac{b}{c}$	
$\left \vec{F}_{s}\right = k\left \vec{x}\right $	$\left \vec{F}_g \right = G \frac{m_1 m_2}{r^2}$	$S = 2\pi r \ell + 2\pi r^2$ Sphere	$\tan \theta = \frac{a}{b}$	
$U_s = \frac{1}{2}kx^2$	$\vec{g} = \frac{F_g}{m}$	$V = \frac{4}{3}\pi r^3$		
$ \rho = \frac{m}{V} $	$U_G = -\frac{Gm_1m_2}{r}$	$S = 4\pi r^2$	b b	

ADVANCED PLACEMENT PHYSICS 1 EQUATIONS, EFFECTIVE 2015

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CONSTANTS AND CONVERSION FACTORS					
Proton mass, $m_p = 1.67 \times 10^{-27} \text{ kg}$	Electron charge magnitude, $e = 1.60 \times 10^{-19} \text{ C}$				
Neutron mass, $m_n = 1.67 \times 10^{-27} \text{ kg}$	1 electron volt, 1 eV = 1.60×10^{-19} J				
Electron mass, $m_e = 9.11 \times 10^{-31} \text{ kg}$	Speed of light, $c = 3.00 \times 10^8 \text{ m/s}$				
Avogadro's number, $N_0 = 6.02 \times 10^{23} \text{ mol}^{-1}$	Universal gravitational constant, $G = 6.67 \times 10^{-11} \text{ m}^3/\text{kg} \cdot \text{s}^2$				
Universal gas constant, $R = 8.31 \text{ J/(mol}\cdot\text{K})$	Acceleration due to gravity at Earth's surface, $g = 9.8 \text{ m/s}^2$				
Boltzmann's constant, $k_B = 1.38 \times 10^{-23} \text{ J/K}$					
1 unified atomic mass unit,	$1 \text{ u} = 1.66 \times 10^{-27} \text{ kg} = 931 \text{ MeV}/c^2$				
Planck's constant,	$h = 6.63 \times 10^{-34} \text{ J} \cdot \text{s} = 4.14 \times 10^{-15} \text{ eV} \cdot \text{s}$				
	$hc = 1.99 \times 10^{-25} \text{ J} \cdot \text{m} = 1.24 \times 10^3 \text{ eV} \cdot \text{nm}$				
Vacuum permittivity,	$\boldsymbol{\varepsilon}_0 = 8.85 \times 10^{-12} \text{ C}^2 / \text{N} \cdot \text{m}^2$				
Coulomb's law constant,	$k = 1/4\pi\varepsilon_0 = 9.0 \times 10^9 \text{ N} \cdot \text{m}^2/\text{C}^2$				
Vacuum permeability,	$\mu_0 = 4\pi \times 10^{-7} \text{ (T-m)/A}$				
Magnetic constant,	$k' = \mu_0 / 4\pi = 1 \times 10^{-7} \text{ (T-m)/A}$				
1 atmosphere pressure,	$1 \text{ atm} = 1.0 \times 10^5 \text{ N/m}^2 = 1.0 \times 10^5 \text{ Pa}$				

UNIT SYMBOLS	meter,	m	mole,	mol	watt,	W	farad,	F
	kilogram,	kg	hertz,	Hz	coulomb,	С	tesla,	Т
	second,	s	newton,	Ν	volt,	V	degree Celsius,	°C
STMBOLS	ampere,	А	pascal,	Pa	ohm,	Ω	electron volt,	eV
	kelvin,	Κ	joule,	J	henry,	Н		

PREFIXES					
Factor	Prefix	Symbol			
10 ¹²	tera	Т			
10 ⁹	giga	G			
10^{6}	mega	М			
10 ³	kilo	k			
10^{-2}	centi	с			
10^{-3}	milli	m			
10^{-6}	micro	μ			
10 ⁻⁹	nano	n			
10^{-12}	pico	р			

VALUES OF TRIGONOMETRIC FUNCTIONS FOR COMMON ANGLES							
θ	0°	30°	37°	45°	53°	60°	90°
$\sin \theta$	0	1/2	3/5	$\sqrt{2}/2$	4/5	$\sqrt{3}/2$	1
$\cos\theta$	1	$\sqrt{3}/2$	4/5	$\sqrt{2}/2$	3/5	1/2	0
$\tan \theta$	0	√3/3	3/4	1	4/3	$\sqrt{3}$	8

The following conventions are used in this exam.

- I. The frame of reference of any problem is assumed to be inertial unless otherwise stated.
- II. In all situations, positive work is defined as work done <u>on</u> a system.
- III. The direction of current is conventional current: the direction in which positive charge would drift.
- IV. Assume all batteries and meters are ideal unless otherwise stated.
- V. Assume edge effects for the electric field of a parallel plate capacitor unless otherwise stated.
- VI. For any isolated electrically charged object, the electric potential is defined as zero at infinite distance from the charged object.

MECHANICS			ELECTRICITY AND MAGNETISM		
$v_x = v_{x0} + x_{x0} + x_{x$	$a_x t$ $a_x t + \frac{1}{2}a_x t^2$	a = acceleration d = distance E = energy E = force	$\left \vec{F}_{E}\right = \frac{1}{4\pi\varepsilon_{0}} \frac{\left q_{1}q_{2}\right }{r^{2}}$ $= -\vec{F}_{E}$	A = area B = magnetic field C = capacitance d = distance	
$v_x^2 = v_{x0}^2 + \sum_{\vec{k}} \vec{k}$	$2a_x(x-x_0)$ \vec{F}	f = force f = frequency h = height I = rotational inertia K = kinetic energy	$E = \frac{1}{q}$ $\left \vec{E}\right = \frac{1}{4\pi\varepsilon_0} \frac{ q }{r^2}$	E = electric field $E = emf$ $F = force$ $L = eurrent$	
$\vec{a} = \frac{\Delta T}{m} = \frac{1}{m}$ $\left \vec{F}_{f}\right \le \mu \left \vec{F}_{n}\right $	$=\frac{1}{m}$	k = spring constant k = spring constant L = angular momentum $\ell = \text{length}$	$\Delta U_E = q \Delta V$ $V = \frac{1}{4\pi\varepsilon_0} \frac{q}{r}$	ℓ = current ℓ = length P = power Q = charge	
$a_c = \frac{v^2}{r}$ $\vec{p} = m\vec{v}$		m = mass $P = power$ $p = momentum$ $r = radius or separation$	$\left \vec{E}\right = \left \frac{\Delta V}{\Delta r}\right $	q = point charge R = resistance r = separation t = time	
$\Delta \vec{p} = \vec{F} \Delta t$ $K = \frac{1}{2} rm^2$		T = period t = time U = potential energy v = speed	$\Delta v = \frac{1}{C}$ $C = \kappa \varepsilon_0 \frac{A}{d}$	U = potential (stored) energy V = electric potential v = speed	
$\Delta E = W =$	$F_{\parallel}d = Fd\cos\theta$	W = work done on a system x = position $\alpha = \text{angular acceleration}$ $\mu = \text{ coefficient of friction}$	$E = \frac{Q}{\varepsilon_0 A}$ $U_C = \frac{1}{2}Q\Delta V = \frac{1}{2}C(\Delta V)^2$	$ \rho = \text{resistivity} $ $ \theta = \text{angle} $ $ \Phi = \text{flux} $	
$P = \frac{\Delta E}{\Delta t}$ $\theta = \theta_0 + \omega_0$	$_{0}t + \frac{1}{2}\alpha t^{2}$	θ = angle τ = torque ω = angular speed	$I = \frac{\Delta Q}{\Delta t}$ $P = \frac{\rho \ell}{2}$	$\vec{F}_M = q\vec{v} \times \vec{B}$	
$\omega = \omega_0 + c$ $x = A\cos(c)$	αt $(\alpha t) = A\cos(2\pi ft)$	$U_s = \frac{1}{2}kx^2$	$R = \frac{1}{A}$ $P = I \Delta V$ ΔV	$\left \vec{F}_{M} \right = \left q \vec{v} \right \left \sin \theta \right \left \vec{B} \right $ $\vec{F}_{M} = I \vec{\ell} \times \vec{B}$	
$x_{cm} = \frac{\sum m}{\sum r}$	$\frac{1}{n_i}$	$T = \frac{2\pi}{\omega} = \frac{1}{f}$	$I = \frac{\Delta Y}{R}$ $R_s = \sum_i R_i$	$\left \vec{F}_{M}\right = \left \vec{\ell}\right \sin\theta \left \vec{B}\right $	
$\vec{\alpha} = \frac{\sum \vec{\tau}}{I} =$ $\tau = r, F =$	$=\frac{\vec{\tau}_{net}}{I}$	$T_s = 2\pi \sqrt{\frac{m}{k}}$	$\frac{1}{R_p} = \sum_i \frac{1}{R_i}$ $C_p = \sum C_i$	$\Phi_B = B \cdot A$ $\Phi_B = \left \vec{B} \right \cos \theta \left \vec{A} \right $	
$L = I\omega$ $\Delta L = \tau \Delta t$		$T_p = 2\pi \sqrt{\frac{-}{g}}$ $\left \vec{F}_g\right = G \frac{m_1 m_2}{r^2}$	$\frac{1}{C_s} = \sum_{i=1}^{i} \frac{1}{C_i}$	$\varepsilon = -\frac{\Delta \Phi_B}{\Delta t}$ $\varepsilon = B\ell v$	
$K = \frac{1}{2}I\omega^2$		$\vec{g} = \frac{\vec{F}_g}{m}$	$B = \frac{\mu_0}{2\pi} \frac{I}{r}$		
$ F_s = k \vec{x} $		$U_G = -\frac{Gm_1m_2}{r}$			

ADVANCED PLACEMENT PHYSICS 2 EQUATIONS, EFFECTIVE 2015

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FLUID MECHANICS A	ND THERMAL PHYSICS	WAVES A	AND OPTICS
FLUID MECHANICS A $\rho = \frac{m}{V}$ $P = \frac{F}{A}$ $P = P_0 + \rho g h$ $F_b = \rho V g$ $A_1 v_1 = A_2 v_2$ $P_1 + \rho g y_1 + \frac{1}{2} \rho v_1^2$ $= P_2 + \rho g y_2 + \frac{1}{2} \rho v_2^2$	ND THERMAL PHYSICS A = area F = force h = depth k = thermal conductivity K = kinetic energy L = thickness m = mass n = number of moles N = number of moles N = number of molesules P = pressure Q = energy transferred to a system by heating T = temperature t = time U = internal energy V = volume	WAVES A $\lambda = \frac{v}{f}$ $n = \frac{c}{v}$ $n_1 \sin \theta_1 = n_2 \sin \theta_2$ $\frac{1}{s_i} + \frac{1}{s_o} = \frac{1}{f}$ $ M = \left \frac{h_i}{h_o}\right = \left \frac{s_i}{s_o}\right $ $\Delta L = m\lambda$ $d \sin \theta = m\lambda$	AND OPTICS d = separation f = frequency or focal length h = height L = distance M = magnification m = an integer n = index of refraction s = distance v = speed $\lambda = \text{wavelength}$ $\theta = \text{angle}$
$\frac{Q}{\Delta t} = \frac{kA \Delta T}{L}$ $PV = nRT = Nk_BT$ $K = \frac{3}{2}k_BT$ $W = -P \Delta V$ $\Delta U = Q + W$	v = volume v = speed W = work done on a system y = height $\rho =$ density	GEOMETRY AND Rectangle A = bh Triangle $A = \frac{1}{2}bh$ Circle $A = \pi r^2$ $C = 2\pi r$	D TRIGONOMETRY A = area C = circumference V = volume S = surface area b = base h = height $\ell = \text{length}$ w = width r = radius
$E = hf$ $K_{\text{max}} = hf - \phi$ $\lambda = \frac{h}{p}$ $E = mc^{2}$	E = energy f = frequency K = kinetic energy m = mass p = momentum $\lambda = wavelength$ $\phi = work function$	Rectangular solid $V = \ell w h$ Cylinder $V = \pi r^2 \ell$ $S = 2\pi r \ell + 2\pi r^2$ Sphere $V = \frac{4}{3}\pi r^3$ $S = 4\pi r^2$	Right triangle $c^2 = a^2 + b^2$ $\sin \theta = \frac{a}{c}$ $\cos \theta = \frac{b}{c}$ $\tan \theta = \frac{a}{b}$ $e^{\frac{1}{b}}$

ADVANCED PLACEMENT PHYSICS 2 EQUATIONS, EFFECTIVE 2015